Solving vector problems

Name:





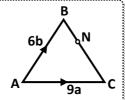
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Find the following vectors in terms of ${\bf a}$ and ${\bf b}$

a) ABC is a triangle.

$$\overrightarrow{BN} = \frac{1}{2}\overrightarrow{NC}$$

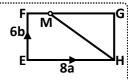
Express \overrightarrow{AN} in terms of **a** and **b**



b) EFGH is a rectangle.

$$\overrightarrow{FM} : \overrightarrow{MG} = 1:3.$$

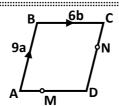
Express \overrightarrow{MH} in terms of **a** and **b**



c) ABCD is a parallelogram.

$$2\overrightarrow{AM} = \overrightarrow{MD}$$
 and $2\overrightarrow{CN} = \overrightarrow{ND}$

Express \overrightarrow{MN} in terms of **a** and **b**



d) PQRS is a parallelogram.

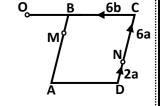
$$\overrightarrow{PX}: \overrightarrow{XS} = 2:3.$$

Y is the midpoint of \overrightarrow{RS} Express \overrightarrow{YX} in terms of **a** and **b**



e) ABCD is a parallelogram. $\overrightarrow{DN} = \mathbf{2a}$ and $\overrightarrow{NC} = \mathbf{6a}$ M is the point on AB such that $\overrightarrow{AM} = 3\overrightarrow{MB}$ OC is a straight line and $\overrightarrow{OB} = \frac{1}{2}\overrightarrow{BC}$

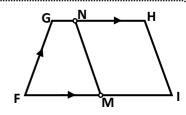
- i) Write an expression for \overrightarrow{MO} in terms of ${\pmb a}$ and ${\pmb b}$
- ii) Determine if OMN is a straight line.



f) FGHI is an isosceles trapezium.

$$\overrightarrow{FG} = \mathbf{2b}$$
, $\overrightarrow{FI} = \mathbf{6a}$, $\overrightarrow{GH} = \mathbf{4a}$, $\overrightarrow{GN} : \overrightarrow{NH} = 1:3$ M is the midpoint of FI

- i) Write an expression for \overrightarrow{HI} in terms of \boldsymbol{a} and \boldsymbol{b}
- ii) Prove that NM is parallel to HI.



Exam question:

ABCD is a parallelogram. $\overrightarrow{AB} = 2a$ and $\overrightarrow{BC} = 4b$ U is the midpoint of AD and T is the midpoint of DC.

- a) Write an expression for \overrightarrow{UT} in terms of \boldsymbol{a} and \boldsymbol{b}
- b) Prove that UT is Parallel to AC.

