Find the values of  $x_1$ ,  $x_2$  and  $x_3$  of the following iterative equations:

a) 
$$x_{n+1} = 2 + \frac{2}{x_n}$$
 and  $x_0 = 1$ 

$$x_1 = 4$$

$$x_2 = 2.5$$

$$x_3 = 2.8$$

d) 
$$x_{n+1} = \frac{5}{3 + (x_n)^2}$$
 and  $x_0 = 0.5$ 

$$x_1 = 1.538461$$

$$x_2 = 0.931643$$

$$x_3 = 1.292672$$

b) 
$$x_{n+1} = 1 + \frac{3}{1+x_n}$$
 and  $x_0 = 1$ 

$$x_1 = 2.5$$

$$x_2 = 1.857142$$

$$x_3 = 2.05$$

e) 
$$x_{n+1} = \frac{x_{n+2}}{x_{n-4}}$$
 and  $x_0 = 0.5$ 

$$x_1 = -0.714285$$

$$x_2 = -0.272727$$

$$x_3 = -0.404255$$

c) 
$$x_{n+1} = 5 - \frac{1}{x_n}$$
 and  $x_0 = 1$ 

$$x_1 = 4$$

$$x_2 = 4.75$$

$$x_3 = 4.789474$$

f) 
$$x_{n+1} = 4 - \frac{2+x_n}{3(x_n)}$$
 and  $x_0 = 0.4$ 

$$x_1 = 6$$

$$x_2 = 4.4444444$$

$$x_3 = 4.48333333$$

Find a solution to these iterative equations correct to 3 significant figures:

g) 
$$x_{n+1} = 2 + \frac{2}{3+x_n}$$
 and  $x_0 = 1$ 

$$x = 2.37$$

h) 
$$x_{n+1} = 3 + \frac{6}{x_n}$$
 and  $x_0 = 2$ 

$$x = 4.37$$

## Exam question:

Using 
$$x_{n+1} = -2 - \frac{2}{(x_n)^2}$$
 with  $x_0 = -1$ 

a) Find the values of 
$$x_1$$
 ,  $x_2$  and  $x_3$ 

$$x_1 = -4$$

$$x_2 = -2.125$$

$$x_3 = -2.442907$$

b) Continue the iteration to find a solution correct to 2 decimal places

