Solving vector problems

Name:





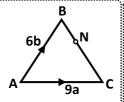
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Find the following vectors in terms of **a** and **b**

a) ABC is a triangle.

$$\overrightarrow{BN} = \frac{1}{2}\overrightarrow{NC}$$

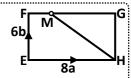
Express \overrightarrow{AN} in terms of **a** and **b**



b) EFGH is a rectangle.

$$\overrightarrow{FM} : \overrightarrow{MG} = 1:3.$$

Express \overrightarrow{MH} in terms of **a** and **b**



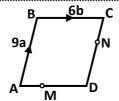
3a + 4b

6a - 6b

c) ABCD is a parallelogram.

$$2\overrightarrow{AM} = \overrightarrow{MD}$$
 and $2\overrightarrow{CN} = \overrightarrow{ND}$

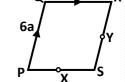
Express \overrightarrow{MN} in terms of **a** and **b**



d) PQRS is a parallelogram.

$$\overrightarrow{PX}: \overrightarrow{XS} = 2:3.$$

Y is the midpoint of \overrightarrow{RS} Express \overrightarrow{YX} in terms of **a** and **b**

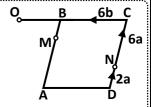


6a + 4b

-3a - 3b

- e) ABCD is a parallelogram. $\overrightarrow{DN} = \mathbf{2a}$ and $\overrightarrow{NC} = \mathbf{6a}$ M is the point on AB such that $\overrightarrow{AM} = 3\overrightarrow{MB}$ OC is a straight line and $\overrightarrow{OB} = \frac{1}{2}\overrightarrow{BC}$
- i) Write an expression for \overrightarrow{MO} in terms of \boldsymbol{a} and \boldsymbol{b}

$$2a + 3b$$



ii) Determine if OMN is a straight line.

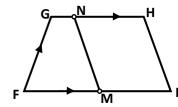
$$\overrightarrow{ON}$$
 = -6a - 9b = -3(2a + 3b) So OMN is a straight line

f) FGHI is an isosceles trapezium.

$$\overrightarrow{FG}=\mathbf{2b}$$
 , $\overrightarrow{FI}=\mathbf{6a}$, $\overrightarrow{GH}=\mathbf{4a}$, $\overrightarrow{GN}:\overrightarrow{NH}=1:3$ M is the midpoint of FI

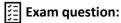
i) Write an expression for \overrightarrow{HI} in terms of \boldsymbol{a} and \boldsymbol{b}

$$2a - 2b$$



ii) Prove that NM is parallel to HI.

$$NM = 2a - 4b = HI$$
 so parallel



ABCD is a parallelogram. $\overrightarrow{AB} = 2a$ and $\overrightarrow{BC} = 4b$ U is the midpoint of AD and T is the midpoint of DC.

a) Write an expression for \overrightarrow{UT} in terms of $m{a}$ and $m{b}$

$$a + 2b$$

b) Prove that UT is Parallel to AC.



